A Statistical Approach for Quantifying Group Difference in Topic Distributions Using Clinical Discourse Samples

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Outline of this presentation

- 1. Motivation
- 2. Describe a statistical approach for explore and quantify topic distributions captured by topic models
- 3. Demonstrate its application using LDA and 2 corpora
 - 20Newsgroups Usenet posts from different topics
 - Clinical corpus Language samples of Autistic* and Typically Developing (TD) children

^{*} We are using identity-first language (i.e., Autistic children) here instead of person-first language (i.e., children with Autism) as the former is the current preference among many Autistic individuals (Brown, n.d.).

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 - Many different topics covered over course of a text or dialogue
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 - To our knowledge, shortage of methods for statistical comparisons
- Latent Dirichlet Allocation (LDA; Blei et al., 2003)
 - Capture and quantify topic distributions for a collection of language samples

Latent Dirichlet Allocation (LDA)

- LDA is a unsupervised, generative probabilistic model that is used on a corpus of text documents to model each document as a finite mixture over k topics
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- Document-topic matrix, heta
 - Each row = single document
 - Each column = single topic
- The elements in θ are the estimated proportion of words in a document that were generated by a given topic

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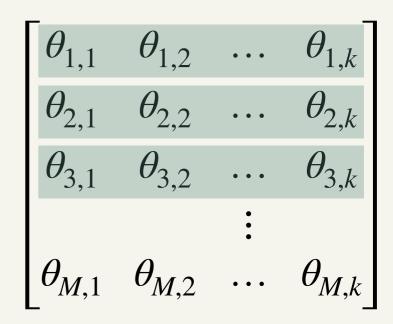
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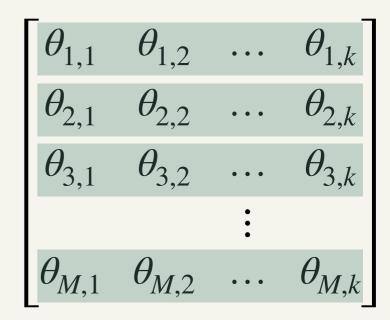
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 To our knowledge, a statistical method for comparing topic distribution vectors between groups of documents has not yet been proposed

- One reason for this is due to certain numerical properties of topic distribution vectors which make them unsuitable for many parametric statistical methods
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 - e.g., the demographic profile of a city, the mineral composition of rocks
- Isometric logratio (ILR) transformation (Egozcue et al., 2003)
 - ILR: $S^D \to \mathbb{R}^{D-1}$
 - Maps compositional data from its original sample space (D-part simplex) into real space (D-1 Euclidean space) with all metric properties preserved
 - After the transformation, we are able to use classical multivariate analysis tools

- Multivariate Analysis of Means (MANOVA)
 - Compares multivariate sample means
 - Requires a number of statistical assumptions to be met before using (described in more detail in the paper)
 - Examines effect of one discrete, independent variable on multiple dependent variables
 - Independent variable —> topic label // diagnostic group
 - Dependent variables —> topic distribution probabilities in the document-topic distribution matrix created by LDA, $\theta_{i,1}, \theta_{i,2}, ..., \theta_{i,k-1}$ where i=1,2,...,M

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- After MANOVA, calculate effect size
 - Partial eta-squared (η^2)
 - What proportion of the variance of the linear combination of topics can be explained by the independent variable

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Statistical Approach

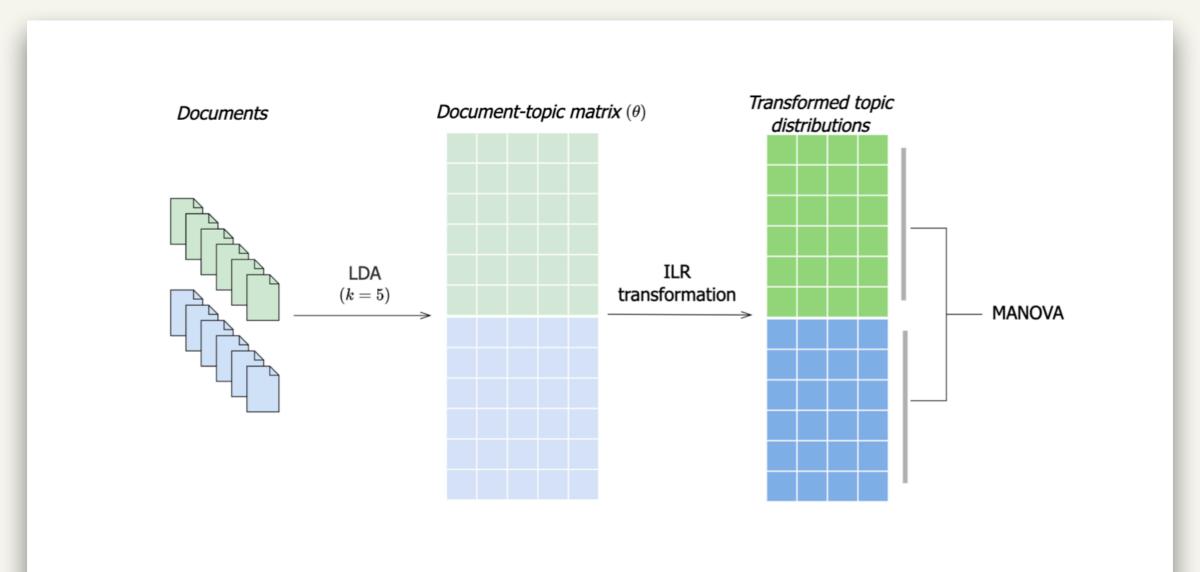


Figure 1: Example workflow for the described statistical approach described to explore and quantify group differences in topic distributions captured by topic models.

- Collection of ~18,000 posts from twenty different Usenet* newsgroups
- Widely used for text classification and analysis

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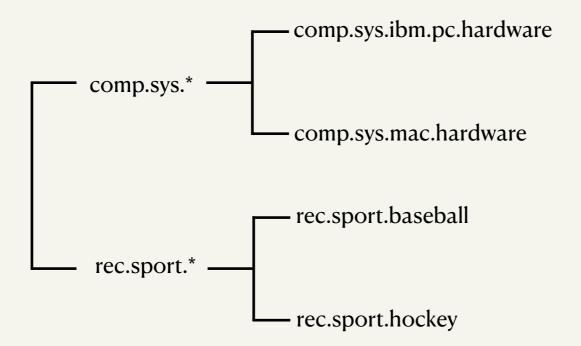
- Collection of ~18,000 posts from twenty different Usenet* newsgroups
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- Used documents from four topics
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 - rec.sport.baseball
 - rec.sport.hockey

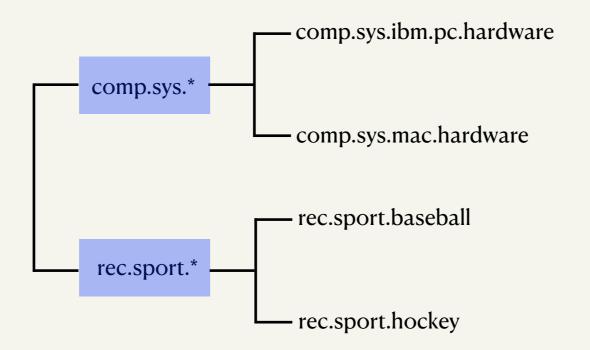
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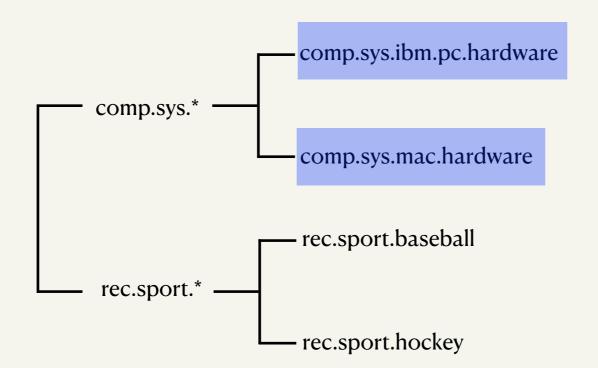
- Fit a single LDA model with a k value of 20
- Transformed topic distribution vectors using ILR transformation
- Checked MANOVA assumptions (detailed in paper)
- Performed 7 MANOVA tests





Between broader categories (x1)

Hypothesis: topic distributions will be very different

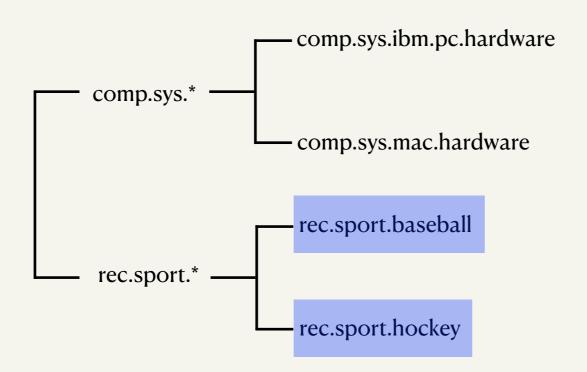


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Hypothesis: topic distributions will also be different, but not as different as previous comparison

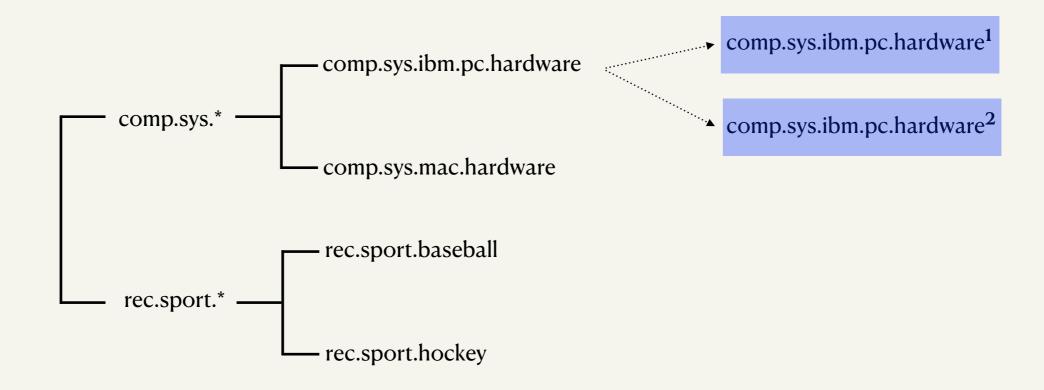


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3. Within a single topic (x4)

Hypothesis: no difference between topic distributions

1. Between broader categories

topics	n	df	Pillai	approx. F	df_1	df_2	p	partial η^2
comp.sys.* rec.sport.*	815 915	1	0.822	414.240	19	1710	<0.001	0.82

Table 2: 20Newsgroups, comparison of LDA topic distribution vectors between and within topics.

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comp.sys.mac.hardware	198 170	1	0.044	0.840	19	348	0.659	0.04
rec.sport.baseball	206 217	1	0.041	0.903	19	403	0.579	0.04
rec.sport.hockey	247 245	1	0.029	0.738	19	472	0.780	0.03

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Clinical corpus (1 of 3)

- Autism Spectrum Disorder (ASD) is a developmental disorder
 - Social communication difficulties, such as problems with topic maintenance
- Sample of 117 ASD and 65 Typically Developing (TD) children, 4 to 15 years old
 - Transcribed dialogues between child and examiner during conversation activities in the ADOS

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 - Social communication difficulties, such as problems with topic maintenance
- Sample of 117 ASD and 65 Typically Developing (TD) children, 4 to 15 years old
 - Transcribed dialogues between child and examiner during conversation activities in the ADOS
- Compare topic distributions in two ways, (1) within child speech (2) within examiner speech
 - For child speech, expect topic distribution vectors of ASD group to be different from those of their TD peers
 - For examiner speech, do not expect topic distributions to differ between ASD and TD groups

Clinical corpus (2 of 3)

- Fit two separate LDA models: one containing child speech and one containing examiner speech
- Document = all words said by a speaker during a single ADOS conversation activity
 - Four activity types —> each child-examiner conversation is associated with four, distinct documents

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- k of 20 used for both models
 - Informed by prior knowledge of type and quantity of questions asked
 - MANOVA tests
 - Independent variable = diagnosis (ASD, TD)
 - Dependent variables = topic probability values from the document-topic vectors
 - Null hypothesis: multivariate means of ASD and TD groups are equal

		df	Pillai	approx. F	df_1	df_2	p	partial η^2
Emotions	dx	1	0.093	0.941	19	175	0.5334	0.09
Social	dx	1	0.188	2.055	19	169	0.0083	0.19
Friends	dx	1	0.131	1.388	19	175	0.1381	0.13
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Future work

- Approach is not restricted to LDA
 - Method can be extended to any topic modeling algorithm that outputs a topic distribution that can be treated as a composition and satisfies the assumption for MANOVA
- Could include additional independent variables by using multivariate analysis of covariance (MANCOVA)
 - For the clinical corpus, participant age, sex, and IQ

Thank you

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Github repo: https://github.com/gracelawley/lawley-sigdial-2023

I am expecting to graduate by the end of 2023 and am on the job market! Grace Olive Lawley
PhD Candidate, Computer Science & Engineering
Oregon Health & Science University
Portland, Oregon, USA

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